

**HOMEWORK #3 – MATH 3210,
FALL 2019**

DUE TUESDAY, SEPTEMBER 10TH

2.1, #4. Guess the limit of the sequence $a_n = \frac{1}{n^2}$ and then prove your guess is correct.

2.1, #6. Guess the limit of the sequence $a_n = \frac{(-1)^n}{n}$ and then prove your guess is correct.

2.1, #8. Guess the limit of the sequence $a_n = \sqrt{n+1} - \sqrt{n}$ and then prove your guess is correct.

2.1, #11. Prove that if $a_n \rightarrow 0$ and k is any constant, then $ka_n \rightarrow 0$.

2.2, #2. Guess the value of $\lim_{n \rightarrow \infty} \frac{n}{n^2+2}$ and then prove your guess is correct.

2.2, #4. Guess the value of $\lim \left(\frac{n}{n+1} \right)^2$ and then prove your guess is correct.

2.2, #9. Does the sequence $\{\cos(n\pi/3)\}$ have a limit? Justify your answer.

2.2, #15. For a certain sequence $\{a_n\}$, there is an $\epsilon > 0$ such that every millionth term of the sequence is greater than ϵ . Can such a sequence converge to zero? Justify your answer.